TzuYu: Learning Stateful Typestates

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Abstract—Behavioral models are useful for various software engineering tasks. They are, however, often missing in practice. Existing work either focuses on learning simple behavioral models such as finite-state automata, or relies on techniques (e.g., symbolic execution) to infer finite-state machines equipped with data states, referred to as stateful typestates. The former is often inadequate as finite-state automata lack expressiveness in capturing behaviors of data-rich programs, whereas the latter is often not scalable. In this work, we propose a fully automated approach to learn stateful typestates by extending the classic active learning process to generate transition guards (i.e., propositions on data states). The proposed approach has been implemented in a tool called TzuYu and evaluated against a number of Java programs. The evaluation results show that TzuYu is capable of learning correct stateful typestates efficiently.

Index Terms—Typestate; Learning; Testing

I. INTRODUCTION

Behavioral models or specifications are useful for various software engineering tasks. For instance, (object) typestates [26], [11], [19], [9] are important for program debugging and verification. A precise (and preferably concise) typestate is useful for understanding third-party programs. In practice, however, such models are often inadequate and incomplete. To overcome this problem, learning based specification mining [4] was proposed to automatically generate behavioral models from various software artifacts, e.g., source code [2], execution traces [21] and natural language API documentations [29]. This approach is promising as it requires no extra user efforts.

Existing approaches on learning typestates (also known as interface specification [3]) can be broadly categorized into two groups. One focuses on learning behavioral models in the forms of finite-state automata, without data states. These methods are often inadequate in practice, as it is known that finite-state automata lack expressiveness in modeling data-rich programs. Consider a simple example of a Stack class with two operations: push and pop. A typestate of the Stack should specify the following language: the number of push operations in any valid trace of the model must be no less than the number of pop operations. It is known that this language is irregular and therefore beyond the expressiveness of finite-state automata. On the other hand, the model of the Stack can be easily expressed using a finite-state machine with a guard condition on the pop operation: size $\geq 1$ where size denotes the number of items in the stack. The central issue is thus: how to identify the proposition size $\geq 1$ systematically and automatically.

The other group learns stateful typestates using relatively heavy-weight techniques like SMT/SAT solving. For instance, in paper [3], the authors proposed to synthesize interface specification for Java classes based on predicate abstraction, which relies on theorem proving. Similarly, in paper [13], the authors propose to learn typestates through symbolic execution (which relies on SMT solving) and refinement. Given that existing theorem proving and SMT/SAT techniques are still limited in handling complicated data structures and control flows, these methods are often limited to small programs.

In this paper, we propose an alternative approach to learning stateful typestates from Java programs. The key idea is to extend an active learning algorithm with an approach to automatically learning transition guards (i.e., propositions on data states). Our approach takes the source code of a class as the only input and generates a stateful typestate through a series of testing, learning and refinement. Fig. 1 shows the high level architecture of our approach. There are three main components. An active learner constructs a typestate based on the L* algorithm [5]. It drives the learning process by generating two kinds of queries. One is membership query, i.e., whether a sequence of events (i.e., a trace) of the current typestate is valid. The other is candidate query, i.e., whether a candidate typestate matches the ‘actual’ typestate. A tester acts as a teacher in the classic active learning setting. It takes queries from the learner and responds accordingly based on testing results. In the original L* algorithm, the model to be learned is a finite-state automaton and a trace can be either valid or invalid but never both. However, in our setting, it is possible that two executions have the same sequences of method calls on the same object but lead to different outcome (i.e., error or no-error), due to different inputs to the method calls (which in turn results in different data states). In such a case, alphabet refinement is performed, by splitting one event into multiple events, each of which has a different guard condition so that the traces are distinguished. The refiner in Fig. 1 is used to automatically identify proper guard conditions. In the following, we use a simple example to illustrate how our method works.

We take the java.util.Stack class in Java (SE 1.4.2) as the running example. Without loss of generality, let us focus on the following two methods: push (which takes an object as an input) and pop, and one data field eleCount (inherited from the java.util.Vector class) which denotes the number of elements in the stack. Initially, we have an alphabet containing two events corresponding to the two methods. Given an
instance of the Stack class, the learner generates a number of membership queries, i.e., a sequence of method calls. Given one membership query, the tester generates multiple test cases which have the same sequence of method calls (with different arguments) and answers the query. The queries and testing results are summarized in the observation table referred to details in Section II-B, as shown in Fig. 2 (a) where the empty sequence of method calls; and denote the sequence of calling after pop. The 0s in column denote that all tests generated for the sequence and then result in an exception or assertion failure (hereafter failure). The 1s denote that none of the tests result in failure. Based on the observation table, the learner generates a candidate typestate as presented in Fig. 2 (b). Note that the typestate is a finite-state automaton with one accepting state, i.e., state A.

Next, the learner asks a candidate query, i.e., is the typestate in Fig. 2 (b) the right typestate? The tester takes the candidate typestate and performs random walking, i.e., randomly generates a set of tests which correspond to traces of the typestate. Notice that a trace of the typestate is either accepting (i.e., ending with an accepting state) or otherwise. Through the random walking, the tester identifies one inconsistency between the typestate and the class under analysis. That is, the typestate predicated that calling from state A always results in failure, whereas it is not always the case. For instance, calling method first (which leads to state A) and then results in no failure.

The existence of inconsistency suggests that the typestate must be refined. We collect data states of the stack at state A before calling method and partition them into two sets, i.e., ones which lead to failure after invoking pop and the rest. Next, the refiner is consulted to generate a proposition such that all data objects in the first set satisfy while all the rest violate . The technique used by the refiner is based on Support Vector Machines (SVMs) [23]. In the above example, the generated proposition is . Next, we re-start the learning process with an alphabet which contains three events: push, and . Then, the condition is satisfied. After a series of membership queries, the learner constructs the observation table as shown in Fig. 3 (a).

Notice that all tests corresponding to result in no failure and therefore it is marked 1 in the table. A new candidate typestate is then generated from the table, as shown in Fig. 3 (b). The tester performs random walking again and finds no inconsistency. We then present Fig. 3 (b) as the resultant typestate after some simple bookkeeping on Fig. 3 (b) by transforming to using the fact that is integer).

The novelty of our approach is on integrating a refiner in the active learning process so as to learn typestates for data-rich programs. In particular, by adopting techniques from machine learning community, we are able to automatically generate propositions for alphabet refinement. The refiner acts as an abstract mapper between the learner and the class under analysis. Compared with existing techniques on finding the right proposition (e.g., [13]), our approach is more scalable as it avoids SMT/SAT encoding and solving. Furthermore, to learn concise stateful typestates efficiently, we investigate the interplay between learning and refinement and develop an algorithm which avoids re-starting learning when alphabet refinement occurs. The method has been implemented in a tool named TzuYu and our experiments show that TzuYu is able to learn meaningful and concise typestates efficiently.

The remainder of the paper is organized as follows. Section II presents preliminary introduction to the concepts and techniques used in our approach. Section III presents the details of our approach. Section IV presents details on the implementation of TzuYu and Section V evaluates its performance with experiments. Section VI discusses related work. Section VII concludes the paper.

II. PRELIMINARIES

In this section we formalize the definitions related to stateful typestate and introduce the techniques used in our approach.

A. Definitions

The input to our method is a Java class (e.g., the Stack class) which is constituted by a set of instance variables (which could

1Who is commonly known as the best student of Confucius.
be objects of other classes) and methods. In this work, we fix one object of the given class as the main receiver and inspect behaviors of all instances of the class through this object. An object state is the status of the object, i.e., the valuation of its variables. For each object, there is an initial object state, i.e., the initial valuation of the variables². A method is a function which takes one object state and returns a new one. A concrete execution ex of an object is a finite sequence

\[ ex = (o_0, m_0(\overline{p_0}), o_1, m_1(\overline{p_1}), \ldots, o_k, m_k(\overline{p_k}), o_{k+1}) \]

where \(o_1\) is an object state and \(m_i(\overline{p_i})\) is a method call with concrete arguments \(\overline{p_i}\). A failed execution is an execution which results in exception or assertion failure. A successful execution is one which does not fail.

The output of our method is a stateful typestate, which is a variant of the deterministic finite-state automaton.

**Definition 1:** A deterministic finite-state automaton (hereafter DFA) is a tuple \(D = (S, \Sigma, \text{init}, \rightarrow, F)\) such that \(S\) is a finite set of states; \(\text{init} \in S\) is an initial state; \(\Sigma\) is an alphabet; \(\rightarrow: S \times \Sigma \rightarrow S\) is a transition function and \(F \subseteq S\) is a set of accepting states.

A trace of \(D\) is a sequence \(tr = (s_0, e_1, s_1, \ldots, s_n, e_n, s_{n+1})\) such that \(s_0 = \text{init}\) and \((s_i, e_i, s_{i+1}) \in \rightarrow\) for all \(i\), \(tr\) is accepting if \(s_{n+1} \in F\). Otherwise, it is non-accepting. The language of \(D\) is the set of all accepting traces of \(D\). In an abuse of notation, we write \(s \xrightarrow{e} s'\) to denote that trace \(tr\) from state \(s\) leads to state \(s'\) and write \(tr(s)\) to denote \(s'\). For two traces \(tr_0\) and \(tr_1\), we write \(tr_0 \cdot tr_1\) to denote their concatenation.

**Definition 2:** A (stateful) typestate of a Java class is a tuple \(T = (\text{Prop}, \text{Meth}, D)\) such that \(\text{Prop}\) is a set of propositions, which are Boolean expressions over variables in the class; \(\text{Meth}\) is the set of method names in the class; \(D = (S, \Sigma, \text{init}, \rightarrow, F)\) is a DFA such that \(\Sigma \subseteq \text{Prop} \times \text{Meth}\).

In the Stack example, a proposition in \(\text{Prop}\) can be constituted by \text{eleCount}, \text{capacity} (inherited from Vector), any data field of \text{elementData} (e.g., \text{elementData.length}), etc. Set \(\text{Meth}\) contains \text{push} and \text{pop}. By definition, typestates are deterministic in this work. Notice that an event in \(\Sigma\) is a pair, i.e., a guard condition \(g\) in \(\text{Prop}\) and a method name \(m\) in \(\text{Meth}\). For brevity, a transition is written as \((s, [g]e, s')\). A typestate abstracts all executions of an object of the class. In particular, a trace \(tr = (s_0, [g_0]e_0, s_1, [g_1]e_1, s_2, \ldots, s_n, [g_n]e_n, s_{n+1})\) is an abstraction of the concrete execution \(ex\) above if they have the same sequence of methods (i.e., \(e_i = m_i\) for all \(i\)) and all the guard conditions are satisfied (i.e., \(g_i\) is satisfied by \(o_1\) and method arguments \(\overline{p_i}\) for all \(i\)). We denote the set of concrete executions of \(tr\) as \(\text{con}(tr)\). Given an execution \(ex\) and an alphabet \(\Sigma\), we can obtain the corresponding trace, denoted as \(\text{abs}(ex)\), by testing which proposition in \(\text{Prop}\) is satisfied for every method call in \(ex\).

A typestate \(D\) is said to be safe (or sound), if for every accepting trace \(tr\) of \(D\), every execution in \(\text{con}(tr)\) is successful.

It is complete if for every concrete execution \(ex\) of the class, there is an accepting trace \(tr\) such that \(ex \in \text{con}(tr)\).

**B. The \(L^*\) Algorithm**

The learner extends the original \(L^*\) algorithm [5] with lazy alphabet refinement, which is introduced latter in section III-C. In the following we introduce the original \(L^*\) algorithm.

The \(L^*\) algorithm assumes that the system to be learned \(D\) is in the form of DFA with a fixed alphabet \(\Sigma\) and learns a DFA with the minimal number of states that accepts the same language of \(D\). During the learning process, the \(L^*\) algorithm interacts with a Minimal Adequate Teacher (teacher for short) by asking two types of queries: membership queries and candidate queries. A membership query asks whether a trace \(tr\) is a trace of \(D\), whereas a candidate query asks whether a DFA \(C\) is equivalent to \(D\), i.e., \(C\) and \(D\) have the same language.

During the learning process, the \(L^*\) algorithm stores the membership query results in an observation table \((P, E, T)\) where \(P \subseteq \Sigma^*\) is a set of prefixes; \(E \subseteq \Sigma^*\) is a set of suffixes; and \(T\) is a mapping function such that \(T(tr, tr') = 1\) if \(tr\) is a trace in \(P\) or a prefix in \(P\) attached with an event in \(\Sigma\); and \(tr'\) is a trace in \(E\) and \(tr \cdot tr'\) is a trace of the system; otherwise, \(T(tr, tr') = 0\). In the observation table, the \(L^*\) algorithm categorizes traces based on Myhill-Nerode Congruence [15].

**Definition 3:** We say two traces \(tr\) and \(tr'\) are equivalent, denoted by \(tr \equiv tr'\), if \(tr \cdot \rho\) is a trace of \(S\) iff \(tr' \cdot \rho\) is a trace of \(S\), for all \(\rho \in \Sigma^*\). Under the equivalence relation, we can say \(tr\) and \(tr'\) are the representing trace of each other with respect to \(S\), denoted by \(tr = [tr']\), and \(tr' = [tr]\).

The \(L^*\) algorithm always tries to make the observation table closed and consistent with membership queries. An observation table is closed if for all \(tr \in P\) and \(e \in \Sigma\), there always exists \(tr' \in P\) such that \(tr \cdot e \equiv tr'\). An observation table is consistent if for every two elements \(tr, tr' \in P\) such that \(tr \equiv tr'\), then \((tr \cdot e) \equiv (tr' \cdot e)\) for all \(e \in \Sigma\). If the observation table \((P, E, T)\) is closed and consistent, the \(L^*\) algorithm constructs a corresponding candidate DFA \(C = (S, \text{init}, \Sigma, \rightarrow, F)\) such that

- \(S\) contains one state for each trace in \(P\); notice that equivalent traces in \(P\) correspond to the same state.
- \(\text{init}\) is the state corresponding to the empty trace \(\epsilon\);
- for any state \(s\) in \(S\) which corresponds to a trace \(tr\) and \(e \in \Sigma\), \((s, e, s') \in \rightarrow\), where \(s'\) is the state for the trace \([tr \cdot e]\), in \(P\);
- a state \(s\) is in \(F\) iff the corresponding trace \(tr\) satisfies \(T(tr) = 1\).

Subsequently, \(L^*\) raises a candidate query on whether \(C\) is equivalent to the system to be learned.

If \(C\) is equivalent to the system, \(C\) is returned as the learning result. Otherwise, the teacher identifies a counterexample, say \(tr\), which is then analyzed to find a witness suffix. A witness suffix is a trace that, when appended to the two traces, provides enough evidence for the two traces to be classified into two equivalence classes under the Myhill-Nerode Congruence. Let
\( tr \) be the concatenation of two traces \( tr_0 \) and \( tr_1 \), i.e., \( tr_0 \cdot tr_1 = tr \). Let \( s \) be the state reached from state \( init \) via trace \( tr_0 \), i.e., \( init \xrightarrow{tr_0} s \). \( tr_1 \) is the witness suffix of \( tr \), denoted by \( WS(tr) \), if \( s \) and \( D(tr) \). Once the witness suffix \( WS(\sigma_{ce}) \) is obtained, \( L^* \) uses \( WS(\sigma_{ce}) \) to refine the candidate DFA \( C \) until \( C \) is equivalent to the system.

Angluin [5] proved that as long as the unknown language \( U \) is regular, the \( L^* \) algorithm will learn an equivalent minimal DFA with at most \( n - 1 \) candidate queries and \( O(\log n) \) membership queries, where \( m \) is the length of the longest counterexample returned by the teacher and \( n \) is the number of states of the minimal DFA.

**Example 1**: We again use the Stack example to illustrate how \( L^* \) works and also why it does not work when the target class cannot be captured by a DFA. After a series of membership queries, \( L^* \) constructs the first candidate DFA, as shown in Fig. 2 (b), and performs a candidate query for the DFA. The teacher answers “no” with a positive counterexample \((push, pop)\), which should be included into the behavior of the candidate. After analyzing the counterexample, the witness suffix \((pop)\) is added into the set of suffixes \( E \) of the observation table, and the closed observation table is shown in Fig. 4 (a). Based on the observation table, \( L^* \) constructs the second candidate DFA, as shown in Fig. 4 (b), and performs a candidate query for the candidate. The teacher answers “no” again with another positive counterexample \((push, push, pop, pop)\). This time, the witness suffix \((pop, pop)\) is added into the set of suffixes \( E \) of the observation table, and the closed observation table is shown in Fig. 5 (a). Based on the observation table, \( L^* \) constructs the third candidate DFA, as shown in Fig. 5 (b), and performs a candidate query for the third one. The reader may find that after the \( i \)-th candidate query for \( i \in \mathbb{N} \), there is always a witness suffix \((pop)^i\) showing that the candidate DFA is incorrect, and one additional state will be added to the candidate DFA, which makes the \( L^* \) learning process non-terminating.

## III. Detailed Approach

In this section we first introduce the detailed design of the tester and refiner and then introduce the learner which interacts with the tester and learner to learn the typestate.

### A. The Tester

The tester acts as the teacher for \( L^* \) algorithm. Ideally, given a membership query for a trace \( tr \), the teacher should answer either yes or no. Since \( tr \) can be mapped into a set of concrete executions \( con(tr) \), that is to say that the teacher should answer yes iff all executions in \( con(tr) \) are successful and answer no iff all executions in \( con(tr) \) are failed. Similarly, given a candidate query, the tester should answer yes iff the candidate typestate is safe and complete.

Having a perfect teacher in our setting is infeasible for two main reasons. Firstly, the set \( con(tr) \) is infinite (with different arguments for method calls) in general and hence checking whether all executions in \( con(tr) \) are successful or not is highly non-trivial. Secondly, it could be that some executions in \( con(tr) \) are successful, whereas some are failed. For instance, assume the class given is \( java.util.Vector \) and \( tr \) is \( \langle addAll \rangle \). A concrete execution with a method call \( addAll \) and argument \( null \) results in exception, whereas a non-null argument results in success. We tackle the former problem by using guided random testing as the teacher, as we discuss below. The latter problem is solved by alphabet refinement, as we show in Section III-B.

In the following, we show how the tester is used as a teacher for membership queries and candidate queries. Given a membership query \( tr \) as follows:

\[
tr = \langle s_0, [g_0]m_0, s_1, [g_1]m_1, s_2, \cdots, s_n, [g_n]m_n, s_{n+1} \rangle
\]

the tester’s task is to identify multiple concrete executions as follows: \( \langle o_0, m_1(p_1^0), o_2, m_2(p_2^0), \cdots, o_k, m_k(p_k^0), o_{k+1} \rangle \). In other words, to automatically generate the arguments for all method calls such that all guard conditions \( g_i \) are satisfied. This task is in general highly non-trivial and requires techniques like SAT/SMT solving. In the name of scalability, we instead apply testing techniques for argument generation. In particular, the approach of Randoop [20] is adopted. In the following, we briefly introduce the idea and refer readers to details in [20].

Given \( tr \), we generate arguments for every method call one-by-one in sequence. Given a typed parameter, the idea is to randomly generate a value from a pool of type-compatible values. This pool composes of a set of pre-defined value (e.g., a random integer for an integer type, \( null \) or an object with the default object state for a user-defined class, etc.) but also type-compatible objects that have been generated during the testing process. We remark that in order to re-create the same object,
we associate each object with the execution which produces the object state. Given one value for each parameter, we then evaluate whether $g_i$ is true or not. If $g_i$ is true, we proceed with next method call.

There are four possible outcomes of the random testing. If all tests are successful, the answer to the query is yes, i.e., $tr$ should be an accepting trace. If all tests are failed, the answer is no, i.e., $tr$ should be a non-accepting trace. If there are both successful tests and failed tests (for $tr$ or a prefix of $tr$), the tests are passed to the refiner for alphabet refinement as we show later. Lastly, due to the limitation of random testing (i.e., the price we pay to avoid theorem proving), it is possible that some guard condition $g_i$ is not satisfied by the generated arguments. In other words, we fail to find any concrete execution in $con(tr)$. In such a case, we optimistically answer yes so that the resultant typestate is more permissive.

To answer a candidate query with a typestate $C$, we use random walk [16], [8], [7] to generate a suite of test cases. Note that the approach of Randooop [20] is again used. Test cases which are inconsistent with the typestates are collected into two sets: positive counterexamples and negative counterexamples. A positive counterexample is a successful test whose corresponding trace $tr$ is non-accepting. A negative example is a failed test whose corresponding trace $tr$ is accepting. If both sets are empty, we answer the query with a yes, i.e., the typestate is the final output. If either of the two sets is not empty, the typestate is ‘invalid’ and a counterexample must be presented to the learner. In the original L* algorithm, presenting any of the counterexample will do. It is however more complicated in our setting as we show below.

For each state $s$ in the typestate $C$, we identify a set of executions in the test suite which end at the state, denoted as $E_s$. For each $e \in \Sigma$, we extend each execution in $E_s$ with a method call corresponding to $e$ and obtain a new set denoted as $E_s^e$. If all of the executions result in failure whereas a transition labeled with $e$ from $s$ leads to an accepting state in $C$, the tester reports that $C$ is invalid and picks one execution in $E_s^e$ and presents its corresponding abstract trace as a counterexample. Similarly, if all of the executions are successful, whereas a transition labeled with $e$ from $s$ leads to a non-accepting state, the tester presents a counterexample. Lastly, if some of the executions in $E_s^e$ result in failure and others result in success, the refiner is consulted to perform alphabet refinement.

B. The Refiner

There are two different scenarios when the refiner is consulted. One is with a membership query $tr$ and a set of tests in $con(tr)$ such that for some of the executions (denoted as $T^-$), performing the last method call (with the generated arguments) results in failure, whereas for the rest of the executions (denoted as $T^+$), performing the last call results in success. In this case, alphabet refinement is a must as all the tests have the same trace $tr$ and therefore they cannot be distinguished without alphabet refinement.

Given an execution in $T^-$ or $T^+$, we can obtain a data state pair $(o, \overline{P})$ where $o$ is the object state of the main instance prior to the last method call and $\overline{P}$ is the list of arguments of the last method call. Let $O^-$ be the set of all pairs we collect from executions in $T^-$ and $O^+$ be the set of all pairs we collect from executions in $T^+$. Intuitively, there must be something different between $O^-$ and $O^+$ such that $T^-$ fails and $T^+$ succeeds. The refiner’s job is to find a divider, in the form of a proposition, such that $O^-$ and $O^+$ can be distinguished. Formally, a divider for $O^+$ and $O^-$ is a proposition $\phi$ such that for all $o \in O^+$, $o$ satisfies $\phi$ and for all $o' \in O^-$, and $o'$ does not satisfy $\phi$. From another point of view, there must be some invariant for all object states in $O^+$ (denoted as $inv^+$) and some invariant for all object states in $O^-$ (denoted as $inv^-$) such that $inv^+$ implies $\phi$ and $inv^-$ implies the negation of $\phi$.

The refiner in our work is based on techniques developed by machine learning community, in particular, Support Vector Machines (SVMs) [23]. SVM is a supervised machine learning algorithm for classification and regression analysis. We use its binary classification functionality. Mathematically, the binary classification functionality of SVMs works as follows. Given two data states (say $O^+$ and $O^-$), each of which can be viewed as a vector of numerical values (e.g., floating-point numbers), it tries to find a separating hyperplane $\Sigma_{i=1}^{n} c_i x_i = c$ such that (1) for every positive data state $(p_1, p_2, \ldots, p_n) \in O^+$ such that $\Sigma_{i=1}^{n} c_i p_i > c$ and (2) for every negative data state $(m_1, m_2, \ldots, m_n) \in O^-$ such that $\Sigma_{i=1}^{n} c_i m_i < c$. As long as $O^+$ and $O^-$ are linear separable, SVM is guaranteed to find a separating hyperplane, even if the invariants $inv^+$ and $inv^-$ may not be linear. Furthermore, there are usually more than one hyperplane that can separate $O^+$ from $O^-$. In this work, we choose the optimal margin classifier (see the definition in [25]) if possible. This separating hyperplane could be seen as the strongest witness why the two data states are different.

In order to use SVM to generate dividers, each element in $O^+$ or $O^-$ must be casted into a vector of numerical types. In general, there are both numerical type (e.g., int) and categorical type (e.g., String) variables in Java programs. Thus, we need a systematic way of mapping arbitrary object states to numerical values so as to apply SVM techniques. Furthermore, the inverse mapping is also important to feedback the SVM results to the original program. Our approach is to systematically generate a numerical value graph from each object type and apply SVM techniques to values associated with nodes in the graph level-by-level. We illustrate our approach using an example in the following.

Fig. 6 shows part of the numerical value graph for type Stack (where many data fields have been omitted for readability). A rectangle (with round corners) represents a categorical type, whereas a circle associated with the type denotes a numerical value which can be extracted from the type. Notice that a categorical type is always associated with a Boolean type value which is true iff the object is null. An edge reads as “contains”. For instance, a Stack type contains an object of type “Array” (i.e., elementData), which in turn contains objects of type “Object”. For readability, each edge is labeled with an abbreviated variable name and each node is labeled with the type. To obtain a vector of numerical values from a type, we
traverse through the graph level-by-level to collect numerical values associated with each type. In general, the graph could be huge if a type contains many variables. For the purpose of typestate learning, however, it is often sufficient to look at only the top few levels.

In the following, we demonstrate how the graph is used. Assume the last event of the membership query is \( \text{true} \implies \text{pop} \) and the two sets of object states are \( O^+ \) and \( O^- \) prior to the method call. Given the receiver object of the method call is a Stack, the refiner first abstracts \( O^+ \) and \( O^- \) using level-0 numerical values in the graph, i.e., \( \text{isNull}, \text{eleCount}, \text{increment} \) and \( \text{increment} \) which is the amount by which the capacity of the vector is automatically incremented when its size becomes greater than its capacity, inherited from the Vector class. Next, the refiner tries to generate a divider which separates the abstracted \( O^+ \) from that of \( O^- \). Assume that \( O^+ \) contains two object states and the abstracted \( O^+ \) is a set: \( \{ (0, 1, 1), (0, 2, 1) \} \) where \( (0, 1, 1) \) denotes a Stack object which is not null (i.e., \( 0 \) means that \( \text{isNull} \) is false), with \( \text{eleCount} \) being 1 and with \( \text{increment} \) being 1. Assume that the abstracted \( O^- \) is: \( \{ (0, 0, 1), (0, 0, 1) \} \). SVM finds a divider \( \text{receiver.eleCount} \geq 1 \). Notice that if there does not exist a linear divider, the refiner refines the abstraction of \( O^+ \) and \( O^- \) by using numerical values from next level in the graph (i.e., \( \text{isNull} \) for \( \text{data} \) and \( \text{length} \) of \( \text{data} \)) and tries again to find a divider. Intuitively, the reason that we look for a divider level-by-level is that we believe that the reason why calling the same method leads to different results is more likely related to the values of variables directly defined in the class and less likely nested in its referenced data variables.

The other scenario where the refiner is consulted is with a candidate query \( C \) and a set of executions which end in the same state in \( C \). Furthermore, extending the executions with a method call corresponding to an event \( e \) would result in failure or success. Similar to the case of a membership query, for each execution we obtain a pair \( (o, \overline{p}) \) where \( o \) is the object state of the main instance prior to the last method call and \( \overline{p} \) is the arguments of the last method call. Similarly, we collect two sets of those pairs \( O^+ \) (from those successful executions) and \( O^- \) (from those failed executions). Afterwards, SVM is invoked to generate a divider for alphabet refinement.

C. The Learner

The learner drives the learning process and interacts with both the tester and refiner. It uses an algorithm which extends the \( \text{L}^* \) algorithm [5] with lazy alphabet refinement.

In general, a typestate for a program often requires more expressiveness than DFA and therefore the \( \text{L}^* \) algorithm itself is not sufficient. We solve this problem by extending the \( \text{L}^* \) algorithm with (lazy) alphabet refinement, i.e., by introducing propositions on object states into the alphabet. The details on the extended \( \text{L}^* \) algorithm are presented in the following.

1) \( \text{L}^* \) with Lazy Alphabet Refinement: When the refiner generates a divider \( \phi \), an event \( e \) (which is the event calling some method under certain condition) is effectively divided into two: \( [\phi]e \) and \( [\neg \phi]e \). With a modified alphabet, previous learning results are invalidated and therefore learning needs to be re-started. However, re-starting from scratch is costly, as we often need multiple rounds of alphabet refinement. In the following, we show how to extend the \( \text{L}^* \) algorithm with lazy alphabet refinement so as to re-use previous learning results as much as possible.

Algorithm 1 shows the pseudo-code of the \( \text{L}^* \) algorithm with lazy alphabet refinement, where \( Q_m(tr) \) denotes the membership query of a trace \( tr \) and \( Q_m(D) \) denotes the candidate query of a typestate \( D \). There are two cases where the alphabet refinement will take place: (1) If a membership query triggers the generation of a divider \( \phi \) (lines 5, 15, 31), some alphabet \( e \in \Sigma \) needs to be split into \( [\phi]e \) and \( [\neg \phi]e \), which calls Algorithm 2 to refine the alphabet and update the corresponding results of the membership queries. (2) A candidate query may also trigger the generation of a divider \( \phi \) (line 24). If so, Algorithm 2 is also called to refine the alphabet and update the corresponding results of the membership queries in the observation table.

We use the Stack example to illustrate the \( \text{L}^* \) algorithm with lazy alphabet refinement. Initially, the alphabet is \( \Sigma = \{ \text{push}, \text{pop} \} \). After a series of memberships, Algorithm 1 constructs the first candidate typestate, as shown in Fig. 2 (b), based on the closed and consistent observation table shown in Fig. 2 (a). A candidate query for the first typestate is performed, and the refiner returns a proposition \( \text{eleCount} \geq 1 \) for the positive counterexample \( \langle \text{pop} \rangle \). The event \( \text{pop} \) is split into two events: \( [\text{eleCount} \geq 1] \text{pop} \) and \( [!\text{eleCount} \geq 1] \text{pop} \), and the \( \text{L}^* \) learning process is started from the scratch. Without lazy alphabet refinement, all the membership queries over the new alphabet \( \Sigma' = \{ \text{push}, \text{eleCount} \geq 1 \} \) have to be queried, as shown in the observation table in Fig. 7. However, with lazy alphabet refinement, only the membership queries marked with a * symbol in the observation table have to be queried. In this small example, only two membership queries are reduced. This is because the alphabet only consists of two events. In real-world examples, the number of alphabet is usually big, and the number of membership queries that can be reduced is significant. The final typestate learned by Algorithm 1 is shown in Fig. 3 (b).
IV. TzuYu Implementation

We have implemented our approach in a tool named TzuYu, which has more than 20K lines of Java code and can be downloaded from the web site [28]. In this section, we discuss the challenges and remedies in implementing the proposed method.

We first employ reflection to collect relevant information like fields and methods of each class so as to construct a numerical value graph for each class. The graph of a type depends on those of the referenced types and hence potentially many types may be referenced. Not all types are useful for the purpose of generating dividers and therefore we filter types like Thread and Exception and high level interfaces such as Serializable. The methods defined in the target class identify the initial alphabet for the learner. Afterwards, the learner starts to generate membership queries and candidate queries according to Algorithm 1.

Given a membership query, the tester checks whether this abstract trace is feasible or not by generating a number (which is configurable) of executions and uses reflection to run them. During the execution, the tester saves the runtime states of the arguments of the trace through instrumentation. For argument generation, we developed a just-in-time approach, i.e., generate the required arguments just before executing a method. Some of the chosen arguments may fail the guard condition, and then we choose another argument which can pass the guard condition. If there is no argument satisfying the condition, we generate another set of arguments until the guard condition evaluates to true (or a bound is reached). We skip the algorithm for the just-in-time generation of arguments. Informally, an argument can be obtained from three sources, i.e., randomly generated from a set of pre-defined type compatible values; selected from existing executions that generate type compatible variables; or selected from type compatible out-referenced variables generated by the current execution. The above recursive argument creation procedure for constructors may not terminate if a constructor has a parameter of the same type as itself. We set a maximum depth of the recursive constructor call in such cases as did in [17].

Before executing of each method call, we store the object states of the receiver and the arguments as a instrumented state. We remark that saving the object state for later usage is not easy in general because its class may not implement Serializable or Cloneable interface. We thus implement a mockup mechanism similar to the standard clone mechanism in Java to save the runtime object into a mockup object whose tree like class structure resembles the class structure of the original object. The mechanism differs from the standard clone mechanism in that only primitive type values of the object are saved. For reference type field we construct another mockup object as its saved value. These mockup objects can be used by

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**Algorithm 1** L* Algorithm with Lazy Alphabet Refinement

1. Let \( P = E = \{()\} \)
2. for \( e \in \Sigma \cup \{()\} \) do
3. Update \( T \) by \( Q_m(e) \)
4. if \( e \) needs to be split then
5. Split(\( \Sigma, e, (P, E, T) \))
6. end if
7. end for
8. while true do
9. while there exists \( tr \cdot \langle e \rangle \) where \( tr \in P \) and \( e \in \Sigma \) such that \( tr \cdot \langle e \rangle \neq tr' \) for all \( tr' \in P \) do
10. \( P \leftarrow P \cup \{tr \cdot \langle e \rangle\} \)
11. for \( e \in \Sigma \) do
12. \( tr'' \leftarrow tr \cdot \langle e \rangle \cdot \langle \sigma \rangle \)
13. Update \( T \) by \( Q_m(tr'') \)
14. if there is some \( e' \in \Sigma \) needs to be split then
15. Split(\( \Sigma, e', (P, E, T) \))
16. end if
17. end for
18. end while
19. Construct candidate typestate \( D \) from \( (P, E, T) \)
20. if \( Q_m(D) = 1 \) then
21. return \( D \)
22. else
23. if there is some \( e' \in \Sigma \) needs to be split then
24. Split(\( \Sigma, e', (P, E, T) \))
25. end if
26. \( v \leftarrow WS(\sigma_{ce}) \quad \triangleright \sigma_{ce} \) is a counterexample
27. \( E \leftarrow E \cup \{v\} \)
28. for \( tr \in P \) and \( e \in \Sigma \) do
29. Update \( T \) by \( Q_m(tr \cdot \langle v \rangle) \) and \( Q_m(tr \cdot \langle \sigma \rangle \cdot \langle v \rangle) \)
30. if there is some \( e' \in \Sigma \) needs to be split then
31. Split(\( \Sigma, e', (P, E, T) \))
32. end if
33. end if
34. end if
35. end while

---

**Algorithm 2** Split

1. Let \( \phi \) be divider given by the Refiner to refine \( e \)
2. \( \Sigma \leftarrow \Sigma \cup \{[\phi]e, [\phi]e \setminus \{e\}\} \)
3. if \( p \in P \) or \( q \in E \) has a substring \( \langle e \rangle \) then
4. split \( p \) into \( p_1 \) and \( p_2 \) such that \( p_1 \) has the substring \( [\phi]e \) and \( p_2 \) has the substring \( [\phi]e \)
5. split \( q \) into \( q_1 \) and \( q_2 \) such that \( q_1 \) has the substring \( [\phi]e \) and \( q_2 \) has the substring \( [\phi]e \)
6. Update \( T \) by \( Q_m(p_i \cdot q_i) \) for all \( i \in \{1, 2\} \)
7. end if

---

**Fig. 7.** The observation table generated by the lazy L* algorithm.
the refiner. If however the real object is needed, for instance, to generate a new test, we record the exact sequence of statements whose execution creates the object that can then be used to “clone” the arguments later by re-executing them.

Given a candidate query, the tester generates a number of tests from the typestate. The default number (which is configurable) is twenty multiplied with the maximum length of traces generated in membership queries before this candidate query. Each testing trace is generated by depth first random walking on the typestate up to a fixed length, the length of the trace is set to two plus the maximum length of traces generated during membership queries. Due to randomness in random testing and random walking, a test case generated previously may not appear again later. To ensure the learning process is improving always (and hopefully converging), we store all the generated test cases so as to provide consistent answers. Notice that we do not store the instrumented states of the test case to reduce memory consumption and we re-execute the test case to create the states when they are needed (e.g., to evaluate the guard conditions).

One key step in our approach is to automatically generate a divider for alphabet refinement. We use the SVM techniques implemented in LibSVM [6]. The first problem with using SVM is how to choose a good hyperplane as there are in theory an infinite set of hyperplanes which separate two sets of object states. The second problem is that the hyperplane discovered by LibSVM often has float number coefficients, which are often not as readable as integer values when we use them to build the typestate. Thus, we always (if possible) choose integer coefficients which constitute a hyperplane which lies between the strongest and weakest hyperplane. Further, we implemented a few heuristics to preprocess the inputs to LibSVM for generating a better divider. Firstly we balance the positive and negative input data sets by duplicating data randomly chosen from the smaller set of the two, as SVM tends to build biased hyperplane when the input data-set is imbalanced.

Secondly, because the arguments of method calls are generated randomly, LibSVM may generate an incorrect divider. For instance, given a Stack with a size bound 5, if \textit{push} is invoked with arguments in \{1, 2, 3\} when there are already 5 items in the stack, whereas it is invoked with arguments in \{5, 6, 7\} when there are less than 5 items in the stack. LibSVM may generate a divider \textit{element} \geq 4 suggesting that calling \textit{push} with an input less than 4 will lead to failure. This is obviously incorrect. The problem is avoided with cross validation by checking whether the argument really affects the execution results. This is done by executing the normal (failed, respectively) traces whose non-receiver arguments are substituted with arguments in the failed (normal, respectively) traces. For instance, in the above example, additional test cases are generated so that every invocation of \textit{push} is tested with the same set of input values, i.e., \{1, 2, 3, 5, 6, 7\}. As a result, if the value is irreverent in determining whether the test fails or succeeds, it will be ruled out by LibSVM.

V. Evaluation

In this section, we first evaluate TzuYu on a set of Java library classes selected from JDK and then compare TzuYu with existing tools. All the experiments were carried out on a Ubuntu 13.04 PC with 2.67 GHz Intel Core i7 Duo processors and 4 GB memory. All the experimental data is available in the web site [28].

The selected JDK classes (from previous related papers [13, 27]) are shown in Table I. Column \textit{LOC} shows the size of the class in terms of lines of code. Column \#\textit{Method} is the number of methods (excluding the constructors of the target class) which are defined in the target class and used to generate the initial alphabet. In this set of experiments, we generate two values for each parameter in each method. To get a numerical vector from an object state (for SVM consumption), we limit the numerical value graphs to its top five levels, which we found to be sufficient.

A. Results

Table I also shows the statistics of the experiments. Column \textit{T_{total}} is the total time used in milliseconds. The subsequent three columns show details about the L* algorithms. Column \#\textit{MQ} and \#\textit{CQ} are the number of membership queries and candidate queries, respectively. Column \#\textit{Trace} is the total number of abstract traces generated from random walking. Column \#\textit{Trace}+ is the number of positive concrete test cases generated by TzuYu. Column \#\textit{SVM} and \textit{T_{SVM}} are the total number of SVM calls and the time in milliseconds taken by SVM to generate dividers, respectively. The last two columns show the size of alphabets and states in the final DFA, respectively.

The following observations are made based on the results. Firstly, TzuYu successfully learned typestates in all cases efficiently, i.e., often in seconds. Furthermore, in most cases, the time taken by SVM is less than 20\% of total time except for \textit{java.io.PipedOutputStream} where the cross validation (in order to determine whether a method parameter is relevant) in a SVM call consumes a few seconds. Secondly, all learned...
TABLE II
PROGRAM INVARIANTS GENERATED BY DAikon, PSYCO AND TzuYu

<table>
<thead>
<tr>
<th>Method</th>
<th>Daikon</th>
<th>PSYCO</th>
<th>TzuYu</th>
</tr>
</thead>
<tbody>
<tr>
<td>java.io.Stack.pop()</td>
<td>-</td>
<td>-</td>
<td>elementCount ≥ 1</td>
</tr>
<tr>
<td>java.util.Stack.peek()</td>
<td>-</td>
<td>-</td>
<td>elementCount ≥ 1</td>
</tr>
<tr>
<td>example.BoundedStack.push(Integer)</td>
<td>size one of {0, 1, 2}</td>
<td>size ≤ 2</td>
<td>size ≥ 1</td>
</tr>
</tbody>
</table>
| java.io.PipedOutputStream.connect(snk)      | size one of {1, 2, 3}       | size ≥ 1                                   | sink == null && snk != null &
|                                             |                             |                                            | & snk.connected == false &
|                                             |                             |                                            | sink != null                                      |
| java.io.PipedOutputStream.write(int)        | sink == null && snk != null | sink == null && snk != null &
|                                             | & snk.connected == false    | & snk.connected == false &
| example.PipedOutputStream.connect(snk)      | sink != null                | sink != null                               |
| example.PipedOutputStream.write(snk)        | Signature VERIFY == state   | Signature.SIGN == state                   | state ≥ 2                                 |
| example.Signature.verify()                  | Signature.SIGN = state      |                                            | state ≥ 1                                 |
| example.Signature.sign()                    | Signature.SIGN < state      |                                            |                                            |

Typestates are sound and complete, which we confirm by comparing the learned one with the manually constructed actual one. Thirdly, the number of states in the learned typestate is minimum, i.e., two as we are differentiating two states only: failure or non-failure. This implies that for every method, whether invoking the method leads to failure or not can be determined by looking at the value of the data variables, and further, SVM is able to identify a suitable proposition every time. Lastly, we did not record the memory consumption due to the garbage collection feature of JVM. However, the memory consumption is relatively small since we did not store the instrumented states with the test cases and the number of test cases is relatively small which are linear in the number of candidate queries.

B. Compare with related tools

We identified three closely related tools. PSYCO [13] is a symbolic execution based typestate learning tool; ADABU [10] is a dynamic behavior model mining framework and Daikon [12] is a dynamic invariant generator. We compare TzuYu with them in terms of time and the quality of the generated models. Table II shows the results of the invariants generated by the three tools and TzuYu. Notice that PSYCO is not available at the time of writing; we thus only obtain the learned typestate documented in their paper [13].

We first compare the models learned by different tools, as shown in Table II. The invariant generated by ADABU are state invariants and they are skipped from Table II. Methods with the trivial true invariant (e.g., size() in Stack) are also omitted. Both ADABU and Daikon need test cases as input to mine models and therefore we use the test cases generated by TzuYu as the input to them for a fair comparison. The number of test cases for each class is shown in the #TC column of Table I. Neither ADABU nor Daikon is able to learn models for all of the classes. For instance, neither mined models for the java.io.PipedOutputStream class. ADABU often generates multiple (e.g., dozens of) models for one class, which means that ADABU cannot merge them to get one final model. That is, ADABU’s state abstraction techniques failed to generate a good invariant. The reason is that ADABU employs a set of pre-defined templates to generate invariants. If a mined state invariant contains irrelevant variables, ADABU’s state abstraction and model merging technique fail and therefore no unified model is generated. In another example, Daikon failed to mine models for java.util.Stack class. Both ADABU and Daikon use pre-defined invariant templates. In comparison, the typestates (which are invariants) generated by TzuYu are better because TzuYu does not rely on templates but rather uses SVM techniques to discover propositions dynamically based on the object states. Furthermore, Daikon uses only successful executions whereas TzuYu uses both successful and failed executions, thus the model learned by TzuYu is more accurate than the one generated by Daikon.

For the two examples (example.PipedOutputStream and example.Signature) which have been reported in paper [13], PSYCO learns accurate transition guards due to the fact that PSYCO encodes all path conditions in the source code and uses SMT solver to find out exactly whether failure happens. PSYCO, however, is limited by the capability of SMT solvers. Next, we compare the execution time of each tool on mining the models briefly. The time taken by each tool to mine the models is plotted in Fig. 8. PSYCO is not available for running the target classes, we cannot get the time for it. Both ADABU and Daikon need test cases while TzuYu generates the test cases, we only include the time consumed by SVM for TzuYu. The figure shows that TzuYu often uses less time in generating.

![Fig. 8. Time consumed in milliseconds to mine models for target classes.](image-url)
the models. An exception is the java.io.PipedOutputStream
class for the reason mentioned above.

C. Limitations of TzuYu

Firstly, because our approach is based on testing, there
is no guarantee on whether the learned typestate is sound
or complete. However, this can be fixed to certain extent
by using an SMT solver to verify the learned typestate.
For instance, the typestate for Stack in Fig. 3 (b) can be
verified by showing that each transition is sound and com-
plete, e.g., the self-looping transition at state 1 labeled with
\[ \text{eleCount} \neq 0 \] \text{pop} \text{can be verified by proving two Hoare
triples:} \{ \text{eleCount} \neq 0 \} \text{pop} \text{(executing pop with
a pre-condition eleCount \neq 0 will not lead to error) and
}\{ \text{eleCount} = 0 \} \text{pop} \text{(error). Further, if an SMT solver
identifies a counterexample, the counterexample can be used
to refine the typestate. We are currently implementing this
verification step in TzuYu.}

Secondly, because our approach is based on random testing,
there is no guarantee that a good divider can be discovered
in general—though it should emerge in theory after sufficient
testing. This can be partially fixed if we can obtain “better”
test cases through different means, e.g., from real execution
history of the given class, or through more sophisticated
test case generation methods like concolic testing [24] and
combinational testing. It is our future work to evaluate the
effectiveness of different test case generation methods in our
setting.

Thirdly, our method will not terminate if the typestate
for the class under analysis is beyond the expressiveness
of finite-state machines with linear guard conditions. If the
refiner fails to find a divider for a membership query with
conflicting results (i.e., same sequence of events leading to
failure sometimes and success sometimes), a counterexample
(i.e., a path which is predicated to fail by the typestate but
succeeds according to the testing result, or the other way
round) is returned so that \text{L*} may introduce a new state. In the
worst case, TzuYu will keep generating typestates with ever
growing number of states (and eventually times out). This is
due to the limitation of SVM that could be overcome using
advanced learning techniques.

VI. RELATED WORK

Our approach is related to specification mining. We refer
interested readers to the book [18] for a comprehensive
literature review. Therefore, we only review previous work
that is closely related to the three components in TzuYu and
the overall approach.

The idea of using testing as a teacher is also found in
paper [14] which combines \text{L*} learning with model check-
ing to check a system against its properties. In case of a
counterexample returned by model checker, it uses testing
based \text{L*} to augment the current model of the system. It
gradually progresses to the final result of either proof or
disproof the system against its properties. The idea of learning
interfaces specifications from source code was proposed in the
seminal paper [3] which learns interface specifications from
source code automatically by using a model checker as the
teacher. The more recent Psyco tool [13] achieves the same
goal by using a symbolic execution engine as the teacher.
In comparison, TzuYu employs testing and thus avoids expensive
model checking or symbolic execution. Similarly, Aarts et
el. [1] proposed a fully automated data abstraction technique
to learn a restricted form of Mealy machine in which only
testing equality of arguments is allowed. TzuYu’s SVM based
alphabet refinement can be applied to more programs.

Our testing strategy is related to the Randoop tool [20]. We
extend Randoop to the context of learning in which the receiv-
er object must be the same in order to learn a better model and
we also add a new source for reference arguments which can
be chosen from an out-reference variables to improve data
coverage. Tester in TzuYu is also related to TAUTOKO [9]
which generates more test cases by mutating existing traces in
the initially mined model (by using ADABU) to augment the
model learning process as well as finding bugs for the class
under test.

We extend the active learning \text{L*} algorithm with lazy
alphabet refinement. There are also other learning algorithms
such as [22]. The sk-strings algorithm [22] passively learns
DFA from a given set of traces by generalizing the method call
sequences in the trace to form the final typestate. ADABU [10]
can be classified as a passive learner which requires a set of
test cases as input, it abstracts the concrete states with simple
templates to abstract states thus to get the abstract traces and
then it merges models from abstract traces to generate a model.
The combination of active learning algorithm with automatic
argument generation techniques enables TzuYu learning state-
ful typestates automatically.

The refiner in TzuYu was inspired by the work [25] which
uses SVM and SMT solver to generate interpolants for coun-
terexamples produced by model checkers. The goal of the
refiner is in line with that of the dynamic invariant generator
Daikon [12] and the tool Axiom Meister [27]. Daikon use a
set of pre-defined invariant templates over data from the set of
given runtime traces. Daikon may find some irrelevant invari-
ants at a program point. The Axiom Meister uses symbolic
execution to collect all the path conditions which are then
abstracted to preconditions. The TzuYu refiner is based on
SVM which enables TzuYu finding relevant linear arithmetic
propositions over a large number of variables.

VII. CONCLUSION

Despite the recent progress on learning specifications from
various software artifacts, the community is still challenged
with difficulties in dealing with data abstraction for common
programs. In this paper, we propose a fully automated types-
tates learning approach from source code. To fully automate
the generation of test cases which are the required inputs for
many automata learning tools, we combine the active learning
algorithm \text{L*} with a random argument generation technique.
We then use a supervised machine learning algorithm (i.e.,
the SVM algorithm) to abstract data into proposition.
REFERENCES


